Hierarchical Formal Verification Using a Hybrid Tool

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\textbf{Abstract.} We describe a hybrid formal hardware verification tool that links the HOL interactive proof system and the MDG automated hardware verification tool. It supports a hierarchical verification approach that mirrors the hierarchical structure of designs. We obtain advantages of both verification paradigms. We illustrate its use by considering a component of a communications chip. Verification with the hybrid tool is significantly faster and more tractable than using either tool alone.

to be simplified, e.g., considering 1-bit instead of 32-bit datapaths. Finding a model reduction and appropriate abstractions so that verification is tractable with the tool can be time-consuming. Moreover, significant detail can be lost. An alternative is interactive theorem proving. The verification can be done hierarchically allowing large designs to be verified without simplification. Furthermore, it is possible to reason about high level abstractions of datatypes. It can however be very time-consuming, requiring significant user interaction and skill.

The contribution of our work is to implement a hybrid tool combining HOL \cite{12} and MDG \cite{3} which provides explicit support for hierarchical hardware verification. In particular, we have provided an embedding of the MDG input language in HOL, implemented a linkage between HOL and MDG using the PROSPER toolkit \cite{9} and implemented a series of HOL tactics that automate hierarchical verification. This means that a hierarchical proof can be performed as it might be done using a pure

1 Introduction

Automated decision diagram based formal hardware verification is fast and convenient, but does not scale well, especially where datapaths and control circuitry are combined. Details of the version of the design verified need
HOL system. However, the MDG tools can be called to perform verification of components that are within its capabilities. We have verified a component of a communication switch using the tool. Verification is shown to be significantly faster and more tractable using the hybrid tool than with either tool individually.

The remainder of this paper is organized as follows. In Section 2 we overview briefly the two tools being linked. We present our hybrid tool and the methodology it embodies in Section 3. A case study using the tool to verify a component of an ATM (Asynchronous Transfer Mode) switch is described in Section 4. Finally, we discuss related work in Section 5 and draw conclusions in Section 6.

2 The Linked Tools

Our hybrid tool links the HOL interactive theorem prover and the MDG hardware verification system. HOL [12] is based on higher-order logic. The user works interactively with the system calling ML functions [19] that implement inference rules to apply proof steps. New theorems are created in HOL by applying inference rules—derived rules call a succession of primitive rules, thus the user can have great confidence in the derived theorems. However, HOL also provides functions to create theorems directly without proof. This feature can be used to import results produced by external tools into HOL. Our hybrid tool uses the PROSPER/Harness Plug-in Inter-

face of HOL [9]. This gives a uniform way of linking HOL with external proof tools. It provides the low level client-server communication interface from HOL to various languages within which other tools are integrated. A range of different external proof tools (such as MDG) can act as servers to a HOL client. The interface removes the burden of writing low-level communication tools, leaving the hybrid tool designer to concentrate on higher-level issues. It also tags theorems produced by plug-ins with a label indicating their source. These labels are propagated to any theorem generated from the imported result allowing the pedigree of any result to be later determined.

The MDG system, which is primarily designed for hardware verification, provides verification procedures for equivalence and property checking. The former provides the verification of two combinational circuits or the verification of two state machines. The latter allows verification through invariant checking or model checking. The strength of the MDG system is its automation and ease of use. It has been used in the verification of significant hardware examples [23, 4, 25]. The MDG system is a decision diagram based verification tool based on Multiway Decision Graphs (MDGs) [5] rather than on binary decision diagrams. MDGs overcome the data width problem of Reduced-Order Binary Decision Diagram (ROBDD) based verification tools. An MDG is a finite, directed acyclic graph (DAG). MDGs essentially represent relations rather than functions. They are much
more compact than ROBDDs for designs containing a
datapath. Furthermore, sequential circuits can be ver-
ified independently of the width of the datapath. The
MDG tools combine some of the advantages of repre-
senting a circuit at more abstract levels with the au-
tomation offered by decision-diagram based tools. The
input language for MDG is MDG-HDL, a simple hard-
ware description language (HDL) supporting structural
descriptions, behavioral descriptions as Abstract State
Machine (ASM) or a mixture of both. A structural de-
scription is usually a netlist of components connected
by signals, and a behavioral description is given by a
tabular representation of the transition/output relation
of the ASM. This is done using the Table construct of
MDG-HDL: essentially a case statement that allows the
value of a variable to be specified in terms of the values
of inputs and other expressions.

3 The Hybrid Tool and Verification
Methodology

In a pure MDG verification, structural and behavioral
descriptions are given for the top level design. An au-
tomated verification procedure is then applied. If the
problem is sufficiently tractable, the verification is com-
pleted automatically. If not, ideally the problem would
be attacked in a hierarchical fashion by verifying the sub-
blocks independently. However, the management of this
process cannot be done within the tool, though could be
done informally outside it.

In a pure HOL hardware verification, the proof is
structured according to the design hierarchy of sub-blocks
within the implementation. For each block, including the
top level block of the design, a structural specification
and behavioral specification are given. Each block’s im-
plementation (apart from those at the bottom of the hi-
erarchy) is verified against its specification in three steps.
Firstly, an intermediate verification result is obtained
about the block based on the behavioral descriptions of
its sub-blocks. Essentially, the sub-blocks are treated as
primitive components in this verification. Secondly, the
process is repeated recursively on the sub-blocks to ob-
tain correctness theorems for them. Finally, the correct-
ness theorems of the sub-blocks are combined with the
intermediate correctness theorem of the block itself to
give the actual correctness theorem of the block. This
is based on the full structural description of the block
down to primitive components. The verification follows
the natural design hierarchy. If this process is applied to
the top level design block, a correctness theorem for the
whole design is obtained. The integration of the verifica-
tion results of the separate components that would be
done informally (if at all) in an MDG verification is thus
formalized and machine-checked in the HOL approach.

Our hybrid tool supports hierarchical verification,
automating the process discussed above, and fits the use
of MDG verification naturally within the HOL frame-
work of compositional hierarchical verification. The HOL system is used to manage the proof, with the MDG system called to verify those design blocks that are tractable. This removes the need to provide behavioral specifications for sub-blocks and the need to verify them separately. In particular, if the design of any sub-block is sufficiently simple, then the hierarchical approach can be abandoned for that block and the whole block verified in one go in MDG. Furthermore, verifying a block under the assumption that its sub-blocks are all primitive components may also be done using MDG if tractable. If not, a normal HOL proof can still be performed. No information is lost in using MDG via the hybrid tool. We use MDG-style behavioral specifications within HOL. This means the specifications must be in the form of a finite state machine or table description. If a higher level abstraction, unavailable in MDG, is required then a separate HOL proof is performed that an MDG style specification meets this abstraction.

3.1 The Hybrid Tool

Our Hybrid tool was written in SML (Standard ML). It consists of five modules: a parsing module, an extraction module, a hierarchical verification support module, a code generation module and an MDG interaction module (cf. Figure 1). Subgoal management is done using the HOL subgoal manager. This is an advantage of the hybrid approach – the existing HOL infrastructure augments MDG providing a much more powerful interface to MDG.

The hybrid tool supports the hierarchical verification process by providing a HOL embedding of the concrete subset of the MDG input language to allow MDG-style specifications to be written in HOL. Several high-level proof tactics that manage and automate the proof process are also provided. A hierarchy tactic, HIER_VERIF_TAC, automates the creation of subgoals from the correctness goal of a block by analyzing its structure as outlined in the previous section. It later combines the proven subgoals to give the desired correctness theorem. Where a non-primitive component occurs several times within a block, the tactic avoids duplication, generating a single subgoal that once proved is automatically instantiated for each occurrence of that component to prove the correctness of the block. Another tactic, MDG_TAC, automates the link to the MDG tools by verifying a given
correctness theorem for a block using MDG combinational or sequential equivalence verification. This is done after analysis of the implementation or specification description. A HOL tactic, BLOCK_VERIF_TAC, has also been developed as part of the hybrid tool that can also verify simple low level blocks automatically, performing Boolean case analysis according to a user-supplied order.

Verification using the hybrid tool proceeds as shown in Figure 2. An initial goal is set that the top level design's implementation meets its behavioral specification. If the design can be verified using MDG, the appropriate MDG tactic, determined by whether the circuit is sequential, is called. Otherwise, the hierarchy tactic is called to break the design into smaller parts, and the process is repeated. At any point, a HOL proof can be performed directly to prove a goal. In general, MDG can fail to terminate due to state-space explosion leading to the system running out of memory or due to certain abstract variables or functions being uninterpreted. This is handled manually within the MDG tool using one of the heuristics described in [3].

3.2 Specifications

The hybrid tool must be supplied with a behavioral specification for each block in the design that is verified. This is not necessary for sub-blocks within blocks verified by calls to MDG. The specifications are intended to be complete specifications covering all aspects of the blocks rather than just partial properties corresponding to some high level property of the whole circuit being verified. The specifications are provided as a normal file of HOL definitions. However, as these definitions must be analyzed by the tool and ultimately converted into MDG, they must follow a prescribed form: they must consist of a conjunction of tables, functional blocks (black-box operations using uninterpreted functions), and input and output arguments must both be explicitly typed and be in a given order. The tables are an embedding of MDG tables in HOL originally defined by Curzon et al. [6] to verify the MDG components in HOL. The verification of these components increases confidence that the MDG tools can be trusted when used in the HOL system.

Structural specifications are written in a subset of the HOL logic similar to that for behavioral specifications. However, the descriptions are not limited to tables but can include any component of the MDG component library. The structural specification of a block thus differs from a behavioral specification in that its body consists
\[
A_j(x, y)(z, \text{cout}) = \\
(MDG\cdot\overline{\text{XOR}}(x, y) z) \land (MDG\cdot\overline{\text{AND}}(x, y) \text{cout})
\]

\[
F_j(x, y, \text{cin})(z, \text{cout}) = \\
\exists z_0 \text{cout}_0 \text{cout}_1.
\]

\[
(MDG\cdot\overline{\text{AND}}(x, y, z_0, \text{cout}_0) z)
\]

\[
(MDG\cdot\overline{\text{OR}}(z_0, \text{cout}_0, \text{cout}_1) \text{cout})
\]

**Fig. 3.** A Structural Specification of an Adder

\[
z_{\text{TAB}}(x, y) z = \\
\text{TABLE }[x:y] z [(F; F); [T; T]] [F:F] T
\]

\[
\text{cout}_0_{\text{TAB}}(x, y) \text{cout} = \\
\text{TABLE }[x:y] \text{cout} [(F; DONT_{\text{CARE}}); [T; F]] [F:F] T
\]

\[
HA(x, y)(z, \text{cout}) = \\
(z_{\text{TAB}}(x, y) z) \land (\text{cout}_0_{\text{TAB}}(x, y) \text{cout})
\]

**Fig. 4.** A Behavioural Specification of a Half-Adder

of a network of components. A component may be an MDG built-in component, a functional block, a table or a component previously defined by the user. The MDG built-in components are an embedding in HOL of the actual MDG components.

### 3.3 The Verification Process

The hybrid tool is intended to provide automated support for hierarchical verification and to enable the user to verify some blocks using MDG. We will illustrate this by referring to the verification of a simple adder circuit. A typical session with the hybrid tool goes through the following steps. First, the user supplies the tool with a specification file and an implementation file as part of an initialization procedure. These are SML files containing normal SML definitions. The specification file includes the behavioral specifications of the design blocks. The implementation file includes the design structural specification and follows the design hierarchy. Both files may include user-defined HOL datatypes. An example of a structural specification for an adder is given in Figure 3.

The behavioral specification of a half-adder in terms of tables is given in Figure 4. The specification of the full adder is similar. In a table specification, the first list gives the inputs of the table, the next argument is the output. Next is a list of lists giving possible combinations of input values and then a list giving the output values resulting from those combinations. The final argument gives the default value for any combination of inputs not listed. MDG tables are more general than shown in this example in that general expressions can be used as table inputs and variables can appear in the rows. We have ommitted type information from this figure (that each variable is a function from time to a Boolean). Strictly, due to the current version of the implementation of the front end of the hybrid tool this information must be provided explicitly, though it would be straightforward to derive it as is done in pure HOL. The initialization procedure also involves loading the embeddings of the MDG tables and the MDG components in HOL as well as starting a server to the MDG system.
Once the tool is initialized, the user sets the correctness goal for the whole design using HOL’s subgoal package. This goal states that the design’s implementation implies its specification. For example, for our adder, we set the goal:

$$\forall x \ y \ cin \ z \ cout.$$ 

$$FA_j (x,y,cin) (z,cout) \implies FA (x,y,cin) (z,cout)$$

This correctness goal could then be resolved directly through MDG using MDG\_TAC. Applying this tactic to complex designs may lead to state explosion. To overcome this, HIER\_VERIF\_TAC is used. The action of this tactic is summarized in Figure 5. It automatically generates a correctness subgoal for every immediate sub-block in the design. Where one sub-block is used in several places, only one goal is generated; the hybrid tool generates a general subgoal that justifies its use in each situation. A further subgoal states that the lower level specifications, connected according to the structural specification, imply the current specification.

For example, HIER\_VERIF\_TAC generates two subgoals for our adder.

$$\forall x \ y \ z \ cout.$$ 

$$HA_j (x,y) (z,cout) \implies HA (x,y) (z,cout)$$

$$\forall x \ y \ cin \ z \ cout.$$ 

$$FA_{j\prime} (x,y,cin) (z,cout) \implies FA (x,y,cin) (z,cout)$$

The first is a correctness statement for the half-adder component. Only one such general theorem is generated. This is used to justify the two slightly different concrete subgoals for the two instances of this component in the design. The second subgoal is a correctness goal for the adder where the half-adder is treated as a primitive component. It contains an automatically generated new structural specification $FA_{j\prime}$, which is in terms of the behavioral specifications of the half-adder submodules rather than their structural specifications:

$$\vdash FA_{j\prime} (x, y, cin) (z, cout) =$$

$$\exists z_0 \ cout_0 \ cout_1$$

$$(HA (x,y) (z_0,cout_0))$$

$$(HA (z_0,cin) (z,cout_1))$$

$$(MDG_{OR} (cout_0,cout_1) \ cout)$$

HIER\_VERIF\_TAC creates a justification function that given theorems corresponding to the subgoals creates the theorem corresponding to the original goal. The subgoals it produces could be resolved using a conventional HOL proof, by invoking MDG as above or by ap-
plying HIER\_VERIF\_TAC once again. If the subgoals are proved, then the justification rule of HIER\_VERIF\_TAC will automatically derive the original correctness goal from them.

When the MDG-based tactics are applied, the hierarchy in the structural specification is automatically flattened to the non-hierarchical form of primitive components required by MDG (just the next layer down in the case of the second subgoal above). The tool currently generates a static variable ordering for use by MDG though more sophisticated ordering heuristics could be included. Alternatively the tool user can provide the ordering. Each block verified can use a different variable ordering.

The tool analyzes the feedback of MDG in order to find out whether the verification succeeded or failed. If the verification fails a counter-example is generated. If it succeeds, the tactic creates the appropriate HOL theorem. For example, for our adder we obtain the theorems:

\[ \text{[MDG]} \vdash \forall x \, y \, z \, \text{cout}. \]

\[ \text{HA} \, j \, (x, y, z, \text{cout}) \implies \text{HA} \, (x, y) \, (z, \text{cout}) \]

\[ \text{[MDG]} \vdash \forall x \, y \, \text{cin} \, z \, \text{cout}. \]

\[ \text{FA} \, j \, j \, \text{l} \, (x, y, \text{cin}, z, \text{cout}) \implies \]

\[ \text{FA} \, (x, y, \text{cin}, (z, \text{cout}) \]

The theorem is tagged with a label indicating its pedigree—that it is proved by an external tool. This tag will be passed to any theorem proved using these theorems.

The theorem proved can be instantiated for any instance. We effectively can prove a single correctness theorem for a block and reuse it for any instance of the block. In our example, there are two instances of the half-adder, but this single theorem is used for both. This process is managed formally and machine-checked within HOL. This contrasts with pure automated tools, where each instance would need a specific theorem to be verified separately or non-machine-checked reasoning to be relied upon. For the half-adder, the subgoals are formally combined using automatic proof by HIER\_VERIF\_TAC to give the desired theorem about the adder:

\[ \text{[MDG]} \vdash \forall x \, y \, \text{cin} \, z \, \text{cout}. \]

\[ \text{FA} \, j \, (x, y, \text{cin}) \, (z, \text{cout}) \implies \]

\[ \text{FA} \, (x, y, \text{cin}) \, (z, \text{cout}) \]

4 Case Study: The 4 \times 4 ATM Switch Fabric

We have applied the hybrid tool to a realistic example: the verification of a block of the Fairisle ATM (Asynchronous Transfer Mode) switch fabric [17]. The Fairisle switch fabric is a real switch fabric designed and used at the University of Cambridge for multimedia applications. It switches cells of data from 4 input ports to 4 output ports as requested by information in header bytes in each cell.

Curzon [8] formally verified this ATM switching element hierarchically using the pure HOL system. However, this verification was very time-consuming. The ver-
ification of the full fabric took approximately two person-months not including the time to develop the formal specifications. Verifying the fabric can be done hierarchically following exactly the same structure as the original design using our hybrid tool. However, with the tool, many of the sub-blocks can be verified automatically using the MDG tool, thus saving a great deal of time and effort. Furthermore, HIER\_VERIF\_TAC automates much of the management of the proof that was previously done manually. Attempting the verification in MDG alone would, on the other hand, be barely tractable taking days of CPU time. This is discussed in more detail below.

Full details of the specifications for the Fabric are given in [8]. As a result various groups have reverified aspects of the circuit using a variety of approaches. For example, Schneider \textit{et al} [21] verified individual blocks of the switch fabric using MEPHISTO. It has also been used as a case study for the Coq system [14]. Garcez [10] verified some properties of the fabric using HSIS and Lu \textit{et al} [18] performed property checking on various abstracted models of the fabric using VIS.

The fabric is split into three sub-blocks, namely Acknowledgement, Arbitration and Data Switch. Further dividing the Arbitration sub-module, we have essentially two blocks: the arbiters that make arbitration decisions and a preprocessing block that generates the timing signal and processes the headers of the cells into a form usable by the arbiters (see Figure 6). We consider the verification of the preprocessor block here (see Figure 7). The timing block within the preprocessor generates a timing signal for the arbiters from an external frame signal and from the data stream. The decoder block (made of 4 independent decoders) takes the four cell headers from the data stream and extracts the information about the destinations they are requesting (which is in a binary encoding). For each destination a unary encoding of the cells that are requesting that output is created. The priority filter takes this information together with priority information from the cell headers. If any cell has high priority, then requests from low priority cells are not forwarded to the arbiters.

Setting as goal the correctness statement for the preprocessor, we attack it using HIER\_VERIF\_TAC\textsuperscript{1}. We obtain two subgoals corresponding to the timing block and the filter-decoder block, together with a subgoal that the combined preprocessor is correct on the assumption that its sub-blocks are. We call MDG\_TAC to automatically prove the timing unit correctness subgoal. This proves the equivalence of the implementation and its specification, and so proves the implication in our subgoal.

Decoders and Priority Filters are purely combinational circuits. Their specifications are the conjunctions of 32 16-input-tables and 16 32-input-tables, respectively. MDG takes 16 hours to verify Decoders and it would

\textsuperscript{1} The specification files and the proof script are available at: 
http://www.ece.concordia.ca/labs/Research/hvg/Tools/Hybrid/ATM
take days to verify *Priority Filters*. The problem is in finding an efficient variable ordering given that the way the sub-blocks are connected means that the best ordering for one table is bad for another. In order to overcome this problem, we move down one level in the design hierarchy. More specifically, the 32 tables in *Decoders*’ specification were partitioned into four 8-table-sub-blocks: *Decoder_IP0* . . . *Decoder_IP3*. *Decoder_IPi* is a decoder for input port *i*, *i* = 0 . . . 3. A more efficient variable ordering is then supplied for each of these sub-blocks. Similarly, the 16 tables in *Priority Filters*’ specification were partitioned into four 4-table-sub-blocks: *Priority_OP0* . . . *Priority_OP3*. *Priority_OPi* is a priority filter for output port *i*, *i* = 0 . . . 3. The preprocessor hierarchy as verified is shown in Figure 7.

We apply HIER_VERIF_TAC to verify *Decoders* and *Priority Filters* based on this hierarchy. The sub-goals associated to *Decoder_IPi* and *Priority_OPi*, *i* = 0 . . . 3, are then proved automatically, in this case using BLOCK_VERIF_TAC. Formal specifications, Curzon [8] originally took sev-
eral days to do the proofs of these blocks using interactive proof whereas the verification is done in minutes using our tool. Verification is also faster than using MDG alone: splitting the decoder block enabled verifying it within less than 1 minute using our hybrid tool instead of 16 hours if only MDG was used. It took a day (approximately 8 hours) to interactively prove the decoder block in HOL. Thus verification is faster using the hybrid tool than with either system on its own as shown in Table 2 which gives approximate times for verifying the decoder block. These times should be treated with caution, as the pure HOL times are not CPU time but that for the human to interactively manage the verification. Times to develop specifications, including those of sub-blocks verified hierarchically rather than directly using MDG, are not included in these times. Writing these specifications was straightforward. It therefore is worthwhile additional work, given the overall time improvement. Some extra human interaction time for the verification part is also needed when using the hybrid tool over the bare CPU time. This is needed to call the

appropriate tactics. However, this is minimal—a matter of minutes rather than hours, since it involves following the existing design hierarchy. The main part that is time consuming is if unsuccessful automated proofs of sub-blocks are attempted. This obviously requires judgement over the limitations of the tools, in knowing when it is worth attempting automated proof, and when it is better to step down a level in the hierarchy.

5 Related Work

Work to combine the advantages of automated and interactive tools falls generally into two areas: hybrid tools in which two existing, stand-alone verification systems are linked; and systems where external proof packages are embedded as decision procedures for some subset of the logic by an interactive system.

Perhaps the most impressive hybrid verification system to date is the combined Voss-ThmTac System [2]. It combines a simple, specially written LCF style proof system, ThmTac with the Voss Symbolic Trajectory Analysis System. This system evolved out of the HOL-VOSS System [15]. In that system, Voss was interfaced within HOL as a tactic that could be called to perform a sym-

<table>
<thead>
<tr>
<th>Block</th>
<th>Size (# 2-input gates)</th>
<th>CPU Time (sec.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Preprocessor</td>
<td>180</td>
<td>495.230</td>
</tr>
<tr>
<td>Timing</td>
<td>18</td>
<td>0.060</td>
</tr>
<tr>
<td>Filter/Decoder</td>
<td>168</td>
<td>480.900</td>
</tr>
<tr>
<td>Decoders</td>
<td>88</td>
<td>45.520</td>
</tr>
<tr>
<td>Decoder DPI</td>
<td>22</td>
<td>10.050</td>
</tr>
<tr>
<td>Priority</td>
<td>80</td>
<td>437.210</td>
</tr>
<tr>
<td>Priority DPI</td>
<td>20</td>
<td>107.413</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th></th>
<th>HOL (Human Proof Time)</th>
<th>MDG (CPU Time)</th>
<th>Hybrid Tool (CPU Time)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Interactive</td>
<td></td>
<td>Automated</td>
<td>Semi-automated</td>
</tr>
<tr>
<td>8 hours</td>
<td></td>
<td>16 hours</td>
<td>1 minute</td>
</tr>
</tbody>
</table>

Table 1. Hierarchical Verification Statistics.

Table 2. Comparison of Verifications of the Decoder Blocks
bolic trajectory analysis to verify assertions about sequences of states. The Voss-Thm/Tac System is thus based on many years of experience combining systems. It has been used to verify a series of real hardware designs including an IA-32 instruction length decoder claimed to be one of the most complex hardware verifications completed. Much of its power comes from the very tight integration of the two provers allowing the user to interact directly with either tool. This is facilitated by the use of a single language, fl, as both the theorem prover’s meta-language and its object language.

Schneider and Hoffmann [22] linked SMV (a CTL model checker) to HOL using PROSPER. In this hybrid tool, HOL conversions were used to transform LTL specifications into ω-Automata, a form that can be reasoned about within SMV. These HOL terms are exported to SMV through the PROSPER plug-in interface. On successful model checking, the results are returned to HOL and turned into tagged theorems. This allows SMV to be used as a HOL decision procedure. The SMV specification language has also been deeply embedded in HOL, allowing CTL specifications to be manipulated in HOL and the model checker user to return a result about its validity.

The use of tightly integrated decision procedures is a major focus of the PVS proof system. Rajan et al [20] integrated a BDD-based model checker for the propositional μ-calculus within PVS. An extension of the μ-calculus is defined within higher-order logic and temporal operators then defined as μ-calculus fixpoint definitions. These expressions are converted into the form required by the model checker which can then be used to prove appropriate subgoals generated within PVS. Such results are treated no differently to those created by proof.

An issue with accepting imported results as theorems is whether the external system can be trusted to produce “theorems” that really are host system theorems. This is more of an issue with fully-expansive proof systems such as HOL where the integrity of the system depends on a small core of primitive inference rules. Accepting results from an external package essentially treats that package as one of the trusted primitives. The approach taken by Gordon [11] to minimize this problem in the BuDDy package when integrating BDD based tools is to provide a small set of BDD primitives in terms of which full tools are implemented. In this way only the primitives need to be trusted not the whole package.

Hurd [13] used PROSPER to combine the Gandalf prover with HOL. Unlike other approaches, the system re proves the Gandalf theorems within HOL rather than just accepting the results. The Gandalf proof script is imported into the HOL system and used to develop a fast proof within HOL. The tool is thus used to discover proofs, rather than directly to prove theorems.

The MEPHISTO system [16] was developed to manage the higher levels of a verification, producing first-order sub-goals to be proved by the FAUST first order
The goals of MEPHISTO are similar to ours: managing the subgoaling of a verification to produce goals that can be proved by another system. The difference is the focus of the way the systems do this and the target system. Our approach is to use the existing design hierarchy, sending to the automated prover (here a hardware verification system itself) subgoals that are correctness theorems about design modules. Thus HIER_VERIF_TAC produces subgoals (and results from failed verification) easily understood by the designer. This approach avoids the problem of the verifier having to inspect goals that bear little relation to the input to the system. MEPHISTO does give some support for hierarchical proof providing a library of preproven modules. However, in our approach such hierarchical verification is explicitly supported by the tactics.

Aagaard et al [1] proposed a similar hardware verification management system. They aimed to complete the whole proof within the theorem prover (HOL or Nuprl). As with MEPHISTO, the focus is on producing lemmas to be proved by decision procedures. They developed a series of prototype tactics that could be used to break down subgoals. However, they do not directly support hierarchical verification: the first step proposed is to rewrite with the module specifications.

As in [2] and [22], we integrate a theorem prover (HOL) to an existing hardware verification tool (MDG) rather than embedding a package within the system. We work within the proof system but using the specification style of the automated tool. This is done by embedding the language of the automated verification tool within the proof system. As is done in pure HOL verification, the proof follows the natural design hierarchy embodied in the specifications. This process is explicitly supported by our hierarchy tactic. The subgoals automatically generated also have a direct relation to the specifications produced by the designer. Thus, the novel aspect of our work is the emphasis on implementing hierarchical verification explicitly in a hybrid tool. The use of MDG as the automated tool also opens up interesting possibilities (not yet fully explored) of making use of its features for abstraction that allow large datapaths to be dealt with automatically.

6 Conclusions

We have described a tool linking an interactive theorem prover and an automated decision diagram-based hardware verification system. This builds on previous work [24], where we showed formally how an MDG equivalence proof can be imported to an implication-based correctness theorem in HOL. Our system explicitly supports the hierarchical compositional verification approach naturally used in interactive proof systems, when using an automated tool. The interactive proof system is used to automatically manage the proof as well as complete any proof interactively that is beyond the scope of the automated system. The verification of whole blocks in
the hierarchy can however be done automatically. The hybrid tool can be used to verify larger examples than could be done in MDG alone, and these proofs can be done faster than in either system alone.

We used the PROSPER/Harness toolkit to perform the linkage of the two tools. This made providing such a linkage relatively easy. However, it took the Harness server minutes to answer requests sent by the proof engine. An alternative implementation that communicated between the tools directly using files was quicker. We are planning to implement the tools' interaction using sockets. This will allow starting multiple instances of MDG on different machines. The hybrid tool will then be responsible of dispatching sub-goals to the MDG instances and collecting verification results back. Load balancing strategies as well as verification workload estimators will be needed to ensure better execution times.

We illustrated the use of the hybrid tool by describing the hierarchical verification of the preprocessing block of the arbitration unit of an ATM switch. Using the hybrid tool, a verification that originally required many hours of interactive proof work, could be done largely automatically using the hybrid tool.

We intend to extend the capabilities of the tool to increase the automation of the proof management process. For example, we will automate different forms of parameterization. Parameterized circuits must currently be dealt with interactively. A single instance of the parameterized circuit is verified using the hybrid tactics and this theorem used in a pure HOL proof of the parameterized circuit—performing the inductive part of the proof [7]. This process could be automated for a range of common parameterization patterns (see Aagaard et al [1]) with a similar tactic to HIER_VERIF_TAC managing the inductive part of the proof. Common abstraction techniques to reduce a model say from 32-bits to 1 bit to make automated verification tractable could also be dealt with in this way. However, MDG provides a better approach: by making fuller use of the abstraction facilities in MDG itself we will remove the need for such abstraction. This removes the need to simplify datapath widths to make verification tractable and enables the handling of data-dependent circuits automatically. We are also in the process of extending the hybrid tool to support model checking in MDG. While most of the infrastructure may be reused, ways of translating and composing properties in HOL need to be developed. For practical reasons industrial designers often do not work to clean hierarchies. Important further work is therefore to integrate a transformational design system with the tool. This would allow non-hierarchical parts of a design to be transformed to a verified equivalent form more conducive to verification, or alternatively to optimise a verified correct hierarchical design in ways that break the verified hierarchy but preserve correctness. Finally, we will consider the verification of more complex examples including a full 16 by 16 switch fabric.
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References


